

(問題8)

2次方程式  $x^2 - x + 1 = 0$  の解の一つを  $\alpha$  とするとき  $\alpha^{5800} + \alpha^{3500} + \alpha^{1700} + \alpha^{70}$  の値を求めよ

(解答)

$$\alpha^2 - \alpha + 1 = 0 \text{ より } \alpha^3 = \alpha^2 \cdot \alpha = (\alpha - 1)\alpha = \alpha^2 - \alpha = -1$$

$$\alpha^{5800} = (\alpha^3)^{1933}\alpha = -\alpha$$

$$\alpha^{3500} = (\alpha^3)^{1166}\alpha^2 = \alpha^2$$

$$\alpha^{1700} = (\alpha^3)^{566}\alpha^2 = \alpha^2$$

$$\alpha^{70} = (\alpha^3)^{23}\alpha = -\alpha$$

$$\alpha^{5800} + \alpha^{3500} + \alpha^{1700} + \alpha^{70} = -\alpha + \alpha^2 + \alpha^2 - \alpha = -2$$